

**Figure 1. (a)** Out-of-plane XRD of C-Er<sub>2</sub>O<sub>3</sub> films with different film thickness. The C-Er<sub>2</sub>O<sub>3</sub>(222) peak becomes sharp and shifts to lower  $2\theta$  values slightly when the film is thicker. (b) Out-of-plane (red square marks with left vertical axis) and in-plane (blue triangle marks with right vertical axis) d-spacing converted from C-Er<sub>2</sub>O<sub>3</sub>(222) and (-440) reflections, respectively, correlating with the film cycle-numbers. (c) The STEM image taken along GaN<11-20> with corresponding C-Er<sub>2</sub>O<sub>3</sub> and GaN projections.