## Supplemental figure for

## Self-referencing photothermal common-path interferometry to augment ellipsometry in low-loss membranes

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**Supplemental figure (a)** Combined optical constants for stoichiometric Si<sub>3</sub>N<sub>4</sub> derived from our experiments using UV-Vis-NIR ellipsometry (230 nm – 2500 nm), mid-IR FTIR spectroscopy (2100 nm – 16  $\mu$ m), and photothermal common-path interferometry (PCI) at 1064 nm. Ellipsometry and FTIR spectroscopy are fast, convenient, and broadband instruments, but are limited in the measurement of loss in low-loss materials. PCI is a sensitive pump-probe technique capable of sub-ppm-level absorption measurements for a particular wavelength. For stoichiometric Si<sub>3</sub>N<sub>4</sub>, the low loss region where ellipsometry and FTIR spectroscopy are not sensitive enough to measure loss is from ~300 nm to ~7  $\mu$ m; estimates of the extinction coefficient vary greatly in this range depending on the oscillator model used. The extinction coefficient measured for a 200-nm-thick Si<sub>3</sub>N<sub>4</sub> membrane using PCI at 1064 nm is shown, which can help pin down the correct model to estimate loss in the low loss region. Experimental setup schematics and photographs for **(b)** ellipsometry, **(c)** photothermal common-path interferometry, and **(d)** FTIR spectroscopy